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TITLE OF INVENTION: Multiple Data Rate Hybrid Walsh Codes for

CDMA

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Currently amended Claims

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for CDMA.

5 INVENTORS: Urbain A. von der Embse

CLAIMS

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WHAT IS CLAIMED IS:

Claim 1. (cancelled)

Claim 2. (cancelled)

Claim 3. (cancelled)

15 Claim 4. (cancelled)

Claim 5. (currently amended) A method for generating and applying hybrid Walsh complex orthogonal codes for code division multiple access (CDMA), said method comprising the steps: the implementation of design and implementation of fast encoders and fast decoders for Hybrid Walsh and generalized Hybrid hybrid Walsh complex orthogonal codes for CDMA, channelization codes for multiple data rate users over said method comprising the steps: a frequency band with properties

generating N Walsh codes W(c) with code index c=0,1,2,...,N-1, each with N chips where N is a power of 2,

generating said N hybrid Walsh codes $\widetilde{W}(c)$ by re-ordering <u>each of said N Walsh codes into a corresponding real component and a corresponding imaginary component of a hybrid Walsh code as defined by equations</u>

for
$$c = 0$$
, $\widetilde{W}(c) = W(0) + jW(0)$
for $c = 1, 2, ..., N/2-1$, $\widetilde{W}(c) = W(2c) + jW(2c-1)$

for c = N/2, $\widetilde{W}(C) = W(N-1) + jW(N-1)$ $\widetilde{W}(c) = W(2N-2c-1)+jW(2N-2c)$ for c = N/2+1,...,N-1, wherein $j=\sqrt{-1}$, wherein said hybrid Walsh codes are generated by reading codethe 5. chip values from saidN Walsh codes chip values from a Walsh code memory in a digital signal processor and writing to said hybrid Walsh memories using a hybrid Walsh code memory using addresses specified by said re-orderings of said N Walsh codes, 10 eedes and, applying said hybrid Walsh codes in the an encoder and in thea decoder of a CDMA system by replacing existing said N Walsh real codes with said hybrid Walsh complex codes using the according to a same code vector indexing., and 15 transmitting data encoded by the encoder and receiving data decoded by the decoder. Hybrid Walsh inphase (real axis) codes and quadrature (imaginary axis) codes are defined by lexicographic reordering permutations of the Walsh code 20 Hybrid Walsh codes have a 1-to-1 sequency frequency correspondence with the DFT codes and have a 1-to-1 even cosine and odd-sine correspondences with the DFT codes

Claim 6. (currently amended) A method for generating and applying spreading codes for code division multiple access (CDMA), comprising the steps: for the implementation of design and implementation of encoders and decoders for complex orthogonal CDMA and hybrid Walsh codes for CDMA as described in claim 5, further comprising the steps: complex orthogonal CDMA

Hybrid Walsh codes take values (1+j, -1+j, -1-j, 1-j) or

equivalently take values {1, j, -1, -j} with a (-45) rotation of

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axes and a renormalization

	chamicifization codes for martiple data rate asers over a
	frequency band with properties
	using tensor products also called Kronecker products to construct
	a second code,
5	constructing a spreading wherein an example 24 chip tensor
	product code from a 8 chip hybrid Walsh code and a 3 chip
	discrete Discrete Fourier transform Transform (DFT) code,
•	said spreading 24 chip code is defined by an 24 N*P row by
	$\frac{24-N*P}{N*P}$ column code matrix C_{24} wherein row vectors are
10	code vectors and column elements are code chips,
	said 8 chip hybrid Walsh code is defined by a 8 N row by 8
	N_column code matrix $-\widetilde{W}_{8}$ _ \widetilde{W} ,
	said $\frac{3 \text{ chip}}{2}$ DFT code is defined by a $\frac{3-P}{2}$ row by $\frac{3-P}{2}$ column
	code matrix E3,
15	said spreading code matrix C_{24} is constructed by tensor a
	Kronecker product of said hybrid Walsh code matrix $\widetilde{\mathtt{W}}$ with
	said DFT code matrix E3 defined by the equation
	$C_{24} = \widetilde{W} \otimes E_3$
	wherein symbol the operator "\omega" is a tensor Kronecker product
20	operation,
	row u+1 and column n+1 matrix element C_{24} (u+1, n+1) of said C_{24} is
	defined by equation
	$\frac{C_{24}(u+1,n+1) - \widetilde{W}_{8}(u_{0}+1,n_{0}+1) - E_{3}(u_{1}+1,n_{1}+1)}{2}$
	wherein
25	
	u 0,1,,23
	$n = n_0 + 8n_1$
	n = 0,1,,23
	wherein u,n are code and chip indices for said codes C24 and
30	u_0, n_0 are code and chip indices for said code \widetilde{W}_{g} and u_1, n_1
	are code and chip indices for said code E37
	wherein said encoder and said decoder for CDMA communications
	have memories assisted to said C. W. F. sadas.

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said C24 codes are generated by reading code chip values from said
           We memory and said E3 memory,
     said chip values are combined using said equations to yield
           said chip values stored in said C24 memory for said C247
  5
     said C24 codes are read from said memory and implemented in said
        - encoder and said decoder,
     using direct products to construct a second code,
     wherein an example 11 chip direct product code is constructed
     - from said 8 chip hybrid Walsh code and said 3 chip DFT
10.
     ---code,
     said 11 chip code is defined by the 11 row by 11 column code
          matrix C<sub>117</sub>
     said C_{11} is constructed by direct product of said \widetilde{W}_k with said E_3
     ____defined by equation
     15
         wherein symbol "⊕" is a direct product operation,
     row u+1 and column n+1 matrix element C11 (u+1,m+1) of said C11 is
           defined by equation
             C_{11}(u+1,n+1) = \widetilde{W}_{k}(u_{0}+1,n_{0}+1) for u=u_{0}, n=n_{0}
                        = E_3(u_1+1,n_1+1) for u=8+u_1, n=8+n_1,
20
                                       ----otherwise,
     wherein said encoder and said decoder for CDMA communications
           qhave memories assigned to said C_{11}, \widetilde{W}_{k}, E_{3} codes,
     said C11 codes are generated by reading code chip values from said
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    memory and said E₃ memory and combined using said

          equations to yield said chip values for said C11 codes and
          stored in said C11 memory,
     said C11 codes are read from memory and implemented in said
           encoder and in said decoder,
30
     using functional combining to construct a second code,
     wherein an example 11 chip functional combined C11 code is
         -constructed from said C_{11} codes by using codes to fill the
        two null subspaces of said C<sub>11</sub>.
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wherein said \hat{c}_{ii} codes are read from memory and implemented in said encoder and said decoder and, using a combinations of tensor products, direct products, and functional combining to construct a second code which is read from memory and implemented in said encoder 5 and said decoder. applying said spreading code matrix C in an encoder and in a decoder of a CDMA system by replacing existing said N Walsh real codes with said hybrid Walsh complex codes according to a same code vector indexing, and 10 transmitting data encoded by the encoder and receiving data decoded by the decoder. Claim 7. (currently amended) A method for implementing the implementation of design and implementation of encoders and 15 decoders for complex orthogonal CDMA and hybrid Walsh codes for CDMA, as described in claim 5, further comprising the steps: said encoder operates as a block encoder, encoding blocks of received N data symbols with contained in a block said with respective N hybrid Walsh codes and 20 summing to yield N chips encoded data symbols for each block at the output chip rate of 1/T chips per second wherein T is the interval between chips, wherein said encoder accepts up to M-N users per block for N-2^M, wherein N is a power of 2 and M is the actual number 25 of users represented in the block, each of said users having a data rate corresponding to one of 1,2,..., N/2 said user data symbols per block, user data symbols over said block are arranged in packets with each packet containing said user data symbols for said 30 -block, wherein said encoder accepts packets from each user and writes them to memory "A" for each block, wherein a binary address index $d=d_0+2d_1+4d_2+...+(N/2)d_{M-1}=0,1,...,N-1$ is

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comprising a number of bits corresponding to the maximum
          number of users N is used for addressing of said data
          symbols stored in memory "A" and the data symbols for each
          user of the block are stored in memory "A" in a hierarchy
          such that a particular user is selected according to a
 5
          number of more significant bits of the binary address index
          and the data symbols of the particular user are selected
          according to a number of lesser significant bits of the
          binary address index, the number of more significant bits
10
          and lesser significant bits of the particular user being
          determined according to the data rate of the particular user
          and the total number of users M per block.
          wherein binary coefficients do, d1, . . . , dM take values
          0.1.
    said binary address index can be independently mapped onto said
15
          data symbol addresses of "A" to provide additional
          flexibility in assigning users to hybrid Walsh vectors,
     said data symbol address is partitioned into M overlapping
          algebraic index fields dw 17 dw 2dw 17. . . , d1d2 . . . dw 2dw 17
          dodid: ----dw-2dw-17 with each field indexed over the allowable
20
          number 2,4,..., N/2, N of said data rate users at symbol
          rates 1/2T,1/4T,...,2/NT,1/NT respectively,
     assign said users with like data symbol rates to the M groups
          u<sub>0</sub>, u<sub>1</sub>, u<sub>1</sub>, u<sub>M-2</sub>, u<sub>M-1</sub>, of users with the respective symbol
          rates 1/2T,1/4T,...,2/NT,1/NT,
25
     assign said data symbol indices in said index field dw to said
          users in said group u0, assign said data symbol indices in
          said index ield d<sub>M 2</sub>d<sub>M 1</sub> to said users in said group u<sub>1</sub>, et
          al and finally assign said data symbol indices in said
          index field dodad2 ... dm 2dm 1 to said users in said group um 17
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     use said mapping and assignments to specify said write addresses
          of said user data symbols onto said input code vector
          stored in said memory "A" and,
     said input vector in said "A" is encoded in said encoder and
              processed for transmission.
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- Claim 8. (currently amended) Wherein said hybrid Walsh codes in claim 5 have a fast encoding implementation algorithm, comprising the steps:
- wherein said fast encoding algorithm implemented in the encoder uses memory "A" for input and to support pass 1 and uses memories "B", "C" to support passes 2, . . . , M wherein N=2^M and uses memory "D" to store the encoded chip output from the reordering pass,
- writing input data symbol vector $Z(d_0, d_1, \ldots, d_{M-2}, d_{M-1})$ to said "A" wherein the binary addressing word takes address values $d_0d_1oood_{M-2}d_{M-1}=0,1,2,\ldots,N-1,$
- wherein pass 1 reads pairs of data symbols from "A" corresponding to d₀=0,1 wherein the addresses of the data symbol for d₀=0 are 0,2,4,...,N-2 and for d₀=1 are 1,3,...,N-1 and for each pair of data symbols pass 1 performs a 2-point hybrid Walsh transform and sums the outputs for each of the encoded chip binary index values n_{M-1}=0,1 and writes the outputs to memory "B" using the addresses of the respective data symbols corresponding to d₀=0,1, and pass 1 processing generates the data vector Z(n_{M-1}, d₁,...,d_{M-1}) in "B",
- wherein pass m=2,3,...,N-1 reads pairs of data symbols from

 "B","C","B",... and writes the outputs to "C","B","C",.

 ... and data symbol pairs for dm-1=0,1 are read over address

 blocks each of length 2^m and starting with the first

 address block the data symbol dm-1=0 is read for addresses

 0,1,,...,2^(m-1) and for dm-1=1 the data symbol addresses are

 2^(m-1)+1,...,2^m and for each pair of data symbols

 pass m performs a 2-point hybrid Walsh transform and sums

 the outputs for each of the encoded chip binary index

 values (nm-m+1 nm-m=0,1) and writes the outputs to addresses

 (nm-m+1,0), (nm-m+1,1) corresponding to the addresses of the

 input dm-1=0,1 and this processing is repeated for each of

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the address blocks and pass m processing generates the
          data vector Z(n_{M-1}, \ldots, n_{M-m}, d_m, \ldots, d_{M-1}),
     wherein pass M reads pairs of data symbols from "B" or "C" and
          writes the output to "C" or "B" and data symbol pairs for
          d_{M-1}=0, 1 are read over addresses 0,1,..., N/2-1 for d_{M-1}=0
 5
          and over addresses N/2, . ., M-1 for d_{M-1}=1 and for each
          pair of data symbols pass M performs a 2-point hybrid Walsh
           transform and sums the outputs for each of the encoded chip
          binary index values (n_1, n_0=0, 1) and writes the output to
          address (n_1,0), (n_1,1) corresponding to the address of the
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           input d_{M-1}=0,1 and pass M processing generates the data
           vector Z(n_{M-1}, \ldots, n_0),
     wherein a final reordering pass re-orders the encoded chip
           symbols in memory "B" or "C" and stores the ordered output
           Z(n_0, n_1, \ldots, n_{M-2}, n_{M-1}) in memory "D", and
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     said fast implementation algorithm in encoder uses said memory
          "A" for input and to support pass 1, memories "B", "C" to
          support passes 2, . . . , M and re-ordering pass, and memory
           "D" for output,
     write input data symbol vector Z(d_0, d_1, \dots, d_{M-2}, d_{M-1}) to said
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           "A" wherein said (d_0, d_1, \dots, d_{M_2}, d_{M_1}) is said binary
           addressing index after said mapping of said data vector
           onto said "A",
     pass 1 reads from said "A", performs pass 1, and writes the
          -output to said "B",
25
     pass 1 multiplies said Z by the kernel [(-1)^dr0nm1+j(-1)^di0
           n_{H,1} and sums over dr_0, di_0=0, 1 to yield the partially
           encoded symbol set Z(n_{M-1}, d_1, \ldots, d_{M-2}, d_{M-1}) where dr_0 = cr(d_0)
           and cr(d) is the real axis Walsh code for d, di0-ci(d0)
           where ci(d) is the imaginary axis Walsh code for d, and n<sub>M-1</sub>
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           is a binary code chip coefficient in said code chip
           indexing n = n_0 + 2n_1 + \dots + (N/4) n_{M-2} + (N/2) n_{M-1}
     write said output symbol set Z(n<sub>M-1</sub>, d<sub>1</sub>, . . . , d<sub>M-2</sub>, d<sub>M-1</sub>) to said
            "B" wherein said address index n<sub>M-1</sub> replaces said index d<sub>0</sub>,
     pass 2 reads from said "B", performs pass 2, and writes the
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output to said "C",
     pass 3 reads from said "C", performs pass 3, and writes the
           output to said "B",
     subsequent passes alternate in read/write from/to said "B" and
 5
          -write/read-to/from-said "C",
     implement passes m=2,3,...,M-1 of said fast encoding algorithm
          by multiplying
           \frac{Z(n_{M-1}, n_{M-2}, \dots, n_{M-m+1}, d_{m-1}, \dots, d_{M-2}, d_{M-1})}{Z(n_{M-1}, n_{M-2}, \dots, n_{M-m+1}, d_{m-1}, \dots, d_{M-2}, d_{M-1})} by the kernel
          - \left\{ (-1)^{dr_{m-1}(n_{M_m} + n_{M_m+1}) + j(-1)^{di_{m-1}(n_{M_m} + n_{M_m+1})} \right\}  and summing
       10
           -\text{set Z}(n_{M-1}, n_{M-1}, n_{M-2}, \dots, n_{M-m}, d_{m}, \dots, d_{M-2}, d_{M-1}),
     implement pass M of said fast encoding algorithm by
          by multiplying Z(n_{M-1}, n_{M-2}, \dots, n_2, n_1, d_{M-1}) by the kernel
          [(-1)^{d_{M_1}}(n_0 + n_1) + j(-1)^{d_{M_1}}(n_0 + n_1)] and summing over
     -----dr<sub>M-1</sub>, di<sub>M-1</sub>=0,1 to yield the encoded symbol set
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           -\frac{2(n_{M-1}-n_{M-1},n_{M-2}-...n_{2},n_{1},n_{0})}{n_{1}}
     reorder said encoded symbol set in memory in the ordered output
           format Z(n_0, n_1, \dots, n_{M-2}, n_{M-1}) and store in said "D" and,
     wherein said encoder in said CDMA transmitter reads said encoded
           symbol chip vector in said "D" and overlays said
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           vector with long and short pseudo-noise (PN) codes to
            generate N chips of said hybrid Walsh encoded said
            data symbol vector for subsequent processing and encoded
            chip vector for transmission.
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Claim 9. (currently amended) Wherein said hybrid Walsh codes in claim 5 have a fast decoding implementation algorithm, comprising the steps:

wherein the decoder strips off said pseudo-noise (PN) codes from the received N chip encoded chip vector and writes the resultant encoded chip vector $Z(n_0, n_1, \ldots, n_{M-2}, n_{M-1})$ to memory "A" wherein the binary addressing word takes address values $n_0 n_1 = 0, 1, 2, \ldots, N-1, \ldots$

wherein said fast decoding algorithm implemented in said decoder uses said memory "A" for input and to support pass 1 and memories "B","C" support passes 2,..., M and memory "D" stores the decoded data symbols from the rescaling and 5 reordering pass, wherein pass 1 reads pairs of encoded chip symbols from "A" corresponding to $n_0=0,1$ wherein the addresses of the chip symbols for $n_0=0$ are 0,2,4,..., N-2 and for $n_0=1$ are 1,3,. . ., N-1 and for each pair of chip symbols pass 1 performs a 10 2-point hybrid Walsh inverse transform and sums the outputs for each of the encoded data symbol index values $d_{M-1}=0,1$ and writes the outputs to memory "B" using the addresses of the respective chip symbols corresponding to $n_0=0,1$ and pass 1 processing generates the vector $Z(d_{M-1}, n_1, \ldots, n_{M-1})$ in 15 "B", wherein pass m=2,3,...,M-1 reads pairs of chip symbols from "B", "C", "B", . . . and writes the outputs to "C", "B", "C", . . . and chip symbol pairs for $n_{m-1}=0,1$ are read over address blocks each of length 2^m, and starting with the first address block the chip symbol $n_{m-1}=0$ is read for addresses 20 $0,1,\dots,2^{(m-1)}$ and for $n_{m-1}=1$ the chip symbol addresses are $2^{(m-1)+1}$, . . ., 2^m and for each pair of chip symbols pass m performs a 2-point hybrid Walsh inverse transform and sums the outputs for each of the decoded data symbol binary index values $(d_{M-m+1}, d_{M-m}=0, 1)$ and writes the outputs to 25 addresses $(d_{M-m+1}, 0)$, $(d_{M-m+1}, 1)$ corresponding to the addressed of the input $n_{m-1}=0,1$ and this processing is repeated for each of the address blocks and pass m processing generates the data vector $Z(d_{M-1}, \ldots, d_{M-m}, n_{m}, \ldots, n_{M-1})$, wherein pass M reads pairs of chip symbols from "B" or "C" and 30 writes the outputs to "C" or "B" and chip symbol pairs for $\underline{n}_{M-1}=0,1$ are read over addresses 0,1,...,N/2-1 for $\underline{n}_{M-1}=0$ and over addresses N/2,...,N-1 for $n_{m-1}=1$ and for each pair of chip symbols pass M performs a 2-point hybrid Walsh inverse transform and sums the outputs for each of the 35

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decoded data symbol binary index values (d_0, d_1=0, 1) and writes the outputs to addresses (d_1, 0), (d_1, 1) corresponding to the addresses of the input n_{M-1}=0, 1, and pass M processing generates the data symbol vector Z(d_{M-1}, \ldots, d_0),
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- wherein a final pass scales the decoded data symbols symbols by
 the N chip hybrid Walsh inverse transform scaling factor
 "1/2N" and re-orders the scaled encoded data symbols in
 memory "B" or "C" and stores the ordered output Z(d₀, d₁,...
 .,d_{M-2}, d_{M-1}) in memory "D", and
- 10 wherein said decoder in said CDMA receiver reads said decoded

 data symbol vector in said "D" for further processing to
 recover information from the data symbols.

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said decoder in said receiver strips off said PN codes from
           said received N chip encoded data symbol vector and outputs
           said received hybrid Walsh encoded chip vector Z(no, ni,...
           -., n<sub>M-2</sub>, n<sub>M-1</sub>) for implementation of said fast decoding
20
           algorithm,
     said fast implementation algorithm in said decoder uses memory
           "E" for input and to support pass 1, memories "F", "G" to
           support passes 2,3,..., M and re-ordering pass, and
           -memory "H" for output,
     25
           (n_0, n_1, \dots, n_{M-2}, n_{M-1}) is the binary address,
     pass 1 reads from said "E", performs pass 1, and writes the
           output to said "F",
     implement pass 1 of said fast decoding algorithm by multiplying
           said Z(n_0, n_1, \dots, n_{M-2}, n_{M-1}) by the kernel (-1)^n_0 dr_{M-1} + j
30
           1) n_0 di_{M-1} and summing over n_0=0,1 to yield the partially
           decoded symbol set
           \frac{Z(d_{M-1}, n_1, \dots, n_{M-2}, n_{M-1})}{}
     write-said output symbol set Z(d<sub>M-1</sub>, n<sub>1</sub>, . . . , n<sub>M-2</sub>, n<sub>M-1</sub>) to said
           "F" wherein address index d<sub>M-1</sub> replaces index n<sub>0</sub>,
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pass 2 reads from said "F", performs pass 2, and writes the
          -output to said "C",
     pass 3 reads from said "G", performs pass 3, and writes the
           output to said "F",
     subsequent passes alternate in read/write from/to said "F" and
 5
           write/read to/from said "G",
     implement passes m=2,3,...,M-1 of said fast decoding algorithm
           by multiplying Z(d_{M-1}, d_{M-2}, \dots, d_{M-m+1}, n_{m-1}, \dots, n_{M-2}, n_{M-1})
           by the kernel
10
     ----[(-1)^n_{m-1}(dr_{M-m}+dr_{M-m+1})+j(-1)^n_{m-1}(di_{M-m}+di_{M-m+1})] and summing
          -over-n<sub>m-1</sub>-0,1 to yield the partially decoded symbol set
          \frac{2(d_{M-1}, d_{M-2}, \dots, d_{M-m}, n_{m}, \dots, n_{M-2}, n_{M-1})}{2}
     implement pass M of said fast decoding algorithm by
            by multiplying Z(d<sub>M-1</sub>, d<sub>M-2</sub>, ..., d<sub>2</sub>, d<sub>1</sub>, n<sub>M-1</sub>) by the kernel
           - \{ (-1)^n_{M+1} (dr_0 + dr_1) + j (-1)^n_{M+1} (di_0 + di_1) \} and summing over
15
            n<sub>M-1</sub>=0,1 and rescaling by dividing by 2N to yield the
            decoded symbol set
            Z(d_{M-1}, -d_{M-1}, d_{M-2}, ..., d_2, d_1, d_0),
     reorder said decoded symbol set in the ordered output format
20
           -\frac{Z(d_{07}-d_{17}, \ldots, d_{M-27}-d_{M-1})}{A} and store in said "H" and,
     said decoder in said receiver reads said decoded symbol vector
           in "D", re-orders the read data symbols to remove said
          -mapping onto said "A", and performs subsequent receive
           signal processing to recover the information from the
25
            data symbols..
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